

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel
Level 3 GCE**

Centre Number

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Candidate Number

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Thursday 6 June 2019

Afternoon (Time: 1 hour 30 minutes)

Paper Reference **9FM0/02**

Further Mathematics

Advanced

Paper 2: Core Pure Mathematics 2

You must have:

Mathematical Formulae and Statistical Tables (Green), calculator

Total Marks

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Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for algebraic manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.
Answers without working may not gain full credit.
- Answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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Answer ALL questions. Write your answers in the spaces provided.

1. (a) Prove that

$$\tanh^{-1}(x) = \frac{1}{2} \ln\left(\frac{1+x}{1-x}\right) \quad -k < x < k$$

stating the value of the constant k .

(5)

(b) Hence, or otherwise, solve the equation

$$2x = \tanh(\ln\sqrt{2-3x})$$

(5)

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Question 1 continued

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(Total for Question 1 is 10 marks)



2. The roots of the equation

$$x^3 - 2x^2 + 4x - 5 = 0$$

are p , q and r .

Without solving the equation, find the value of

(i) $\frac{2}{p} + \frac{2}{q} + \frac{2}{r}$

(ii) $(p - 4)(q - 4)(r - 4)$

(iii) $p^3 + q^3 + r^3$

(8)



Question 2 continued

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(Total for Question 2 is 8 marks)



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Question 3 continued

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(Total for Question 3 is 6 marks)



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4. The infinite series C and S are defined by

$$C = \cos \theta + \frac{1}{2} \cos 5\theta + \frac{1}{4} \cos 9\theta + \frac{1}{8} \cos 13\theta + \dots$$

$$S = \sin \theta + \frac{1}{2} \sin 5\theta + \frac{1}{4} \sin 9\theta + \frac{1}{8} \sin 13\theta + \dots$$

Given that the series C and S are both convergent,

(a) show that

$$C + iS = \frac{2e^{i\theta}}{2 - e^{4i\theta}} \quad (4)$$

(b) Hence show that

$$S = \frac{4\sin \theta + 2\sin 3\theta}{5 - 4\cos 4\theta} \quad (4)$$



5. An engineer is investigating the motion of a sprung diving board at a swimming pool. Let E be the position of the end of the diving board when it is at rest in its equilibrium position and when there is no diver standing on the diving board. A diver jumps from the diving board. The vertical displacement, h cm, of the end of the diving board above E is modelled by the differential equation

$$4 \frac{d^2h}{dt^2} + 4 \frac{dh}{dt} + 37h = 0$$

where t seconds is the time after the diver jumps.

- (a) Find a general solution of the differential equation. (2)

When $t = 0$, the end of the diving board is 20 cm below E and is moving upwards with a speed of 55 cm s^{-1} .

- (b) Find, according to the model, the maximum vertical displacement of the end of the diving board above E . (8)

- (c) Comment on the suitability of the model for large values of t . (2)



Question 5 continued

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6. In an Argand diagram, the points A , B and C are the vertices of an equilateral triangle with its centre at the origin. The point A represents the complex number $6 + 2i$.
- (a) Find the complex numbers represented by the points B and C , giving your answers in the form $x + iy$, where x and y are real and exact. (6)

The points D , E and F are the midpoints of the sides of triangle ABC .

- (b) Find the exact area of triangle DEF . (3)



7.

$$\mathbf{M} = \begin{pmatrix} 2 & -1 & 1 \\ 3 & k & 4 \\ 3 & 2 & -1 \end{pmatrix} \quad \text{where } k \text{ is a constant}$$

(a) Find the values of k for which the matrix \mathbf{M} has an inverse. (2)

(b) Find, in terms of p , the coordinates of the point where the following planes intersect

$$2x - y + z = p$$

$$3x - 6y + 4z = 1$$

$$3x + 2y - z = 0$$

(5)

(c) (i) Find the value of q for which the set of simultaneous equations

$$2x - y + z = 1$$

$$3x - 5y + 4z = q$$

$$3x + 2y - z = 0$$

can be solved.

(ii) For this value of q , interpret the solution of the set of simultaneous equations geometrically. (4)



Question 8 continued

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Question 8 continued

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Question 8 continued

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Question 8 continued

Horizontal lines for writing answers.

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(Total for Question 8 is 11 marks)

TOTAL FOR PAPER IS 75 MARKS

