

Paper 2 Option J

Further Mechanics 1 Mark Scheme (Section A)

Question	Scheme	Marks	AOs
1(a)	Using the model and $v^2 = u^2 + 2as$ to find v	M1	3.4
	$v^2 = 2as = 2g \times 2.4 = 4.8g \Rightarrow v = \sqrt{4.8g}$	A1	1.1b
	Using the model and $v^2 = u^2 + 2as$ to find u	M1	3.4
	$0^2 = u^2 - 2g \times 0.6 \Rightarrow u = \sqrt{1.2g}$	A1	1.1b
	Using the correct strategy to solve the problem by finding the sep. speed and app. speed and applying NLR	M1	3.1b
	$e = \sqrt{1.2g} / \sqrt{4.8g} = 0.5$ *	A1*	1.1b
	(6)		
(b)	Using the model and $e = \text{sep. speed} / \text{app. speed}$, $v = 0.5\sqrt{1.2g}$	M1	3.4
	Using the model and $v^2 = u^2 + 2as$	M1	3.4
	$0^2 = 0.25(1.2g) - 2gh \Rightarrow h = 0.15$ (m)	A1	1.1b
		(3)	
(c)	Ball continues to bounce with the height of each bounce being a quarter of the previous one	B1	2.2b
		(1)	
(10 marks)			
Notes:			
(a)	M1: For a complete method to find v A1: For a correct value (may be numerical) M1: For a complete method to find u A1: For a correct value (may be numerical) M1: For finding both v and u and use of Newton's Law of Restitution A1*: For the given answer		
(b)	M1: For use of Newton's Law of Restitution to find rebound speed M1: For a complete method to find h A1: For 0.15 (m) oe		
(c)	B1: For a clear description including reference to a quarter		

Question	Scheme	Marks	AOs
2(a)	Energy Loss = KE Loss – PE Gain	M1	3.3
	$= \frac{1}{2} \times 0.5 \times 25^2 - 0.5 g \times 20$	A1	1.1b
	$= 58.25 = 58 \text{ (J) or } 58.3 \text{ (J)}$	A1	1.1b
		(3)	
(b)	Using work-energy principle, $20 R = 58.25$	M1	3.3
	$R = 2.9125 = 2.9 \text{ or } 2.91$	A1ft	1.1b
		(2)	
(c)	Make resistance variable (dependent on speed)	B1	3.5c
		(1)	
(6 marks)			
Notes:			
(a)			
M1: For a difference in KE and PE			
A1: For a correct expression			
A1: For either 58 (2sf) or 58.3(3sf)			
(b)			
M1: For use of work-energy principle			
A1ft: For either 2.9 (2sf) or 2.91 (3sf) follow through on their answer to (a)			
(c)			
B1: For variable resistance oe			

Question	Scheme	Marks	AOs
3(a)	Force = Resistance (since no acceleration) = 30	B1	3.1b
	Power = Force \times Speed = 30 \times 4	M1	1.1b
	= 120 W	A1 ft	1.1b
		(3)	
(b)	Resolving parallel to the slope	M1	3.1b
	$F - 60g\sin\alpha - 30 = 0$	A1	1.1b
	$F = 70$	A1	1.1b
	Power = Force \times Speed = 70 \times 3	M1	1.1b
	= 210 W	A1 ft	1.1b
		(5)	
(8 marks)			
Notes:			
<p>(a) B1: For force = 30 seen M1: For use of $P = Fv$ A1ft: For 120 (W), follow through on their '30'</p>			
<p>(b) M1: For resolving parallel to the slope with correct no. of terms and 60g resolved A1: For a correct equation A1: For $F = 70$ M1: For use of $P = Fv$ A1ft: For 210 (W), follow through on their '70'</p>			

Question	Scheme	Marks	AOs
4(a)	Use of conservation of momentum	M1	3.1a
	$3mu - 2mu = 3mv + mw$	A1	1.1b
	Use of NLR	M1	3.1a
	$3ue = -v + w$	A1	1.1b
	Using a correct strategy to solve the problem by setting up two equations (need both) in u and v and solving for v	M1	3.1b
	$v = \frac{u}{4}(1 - 3e)$	A1	1.1b
		(6)	
(b)	$\frac{u}{4}(1 - 3e) < 0$	M1	3.1b
	$\frac{1}{3} < e \leq 1$	A1	1.1b
		(2)	
(c)	Solving for w	M1	2.1
	$w = \frac{u}{4}(1 + 9e)^*$	A1 *	1.1b
		(2)	
(d)	Substitute $e = \frac{5}{9}$	M1	1.1b
	$v = -\frac{u}{6}, w = \frac{3u}{2}$	A1	1.1b
	Use NLR for impact with wall, $x = fw$	M1	1.1b
	Further collision if $x > -v$	M1	3.4
	$f \frac{3u}{2} > \frac{u}{6}$	A1	1.1b
	$1 \geq f > \frac{1}{9}$	A1	1.1b
		(6)	

(16 marks)

Notes:

(a)

M1: For use of CLM, with correct no. of terms, condone sign errors

A1: For a correct equation

M1: For use of Newton's Law of Restitution, with e on the correct side

A1: For a correct equation

M1: For setting up *two* equations and solving their equations for v

A1: For a correct expression for v

(b)

M1: For use of an appropriate inequality

A1: For a complete range of values of e

(c)

M1: For solving their equations for w

A1: For the given answer

Question 4 notes continued:

(d)

M1: For substituting $e = \frac{5}{9}$ into their v and w

A1: For correct expressions for v and w

M1: For use of Newton's Law of Restitution, with e on the correct side

M1: For use of appropriate inequality

A1: For a correct inequality

A1: For a correct range

Further Mechanics 2 Mark Scheme (Section B)

Question	Scheme	Marks	AOs
5 (a)	Multiply out and differentiate wrt t	M1	1.1b
	$v = 3t^2 - 16t + 20 \Rightarrow a = 6t - 16$	A1	1.1b
		(2)	
(b)	Multiply out and integrate wrt t	M1	1.1b
	$s = \int 3t^2 - 16t + 20dt = t^3 - 8t^2 + 20t(+C)$	A1	1.1b
	$t = 0, s = 0 \Rightarrow C = 0$ $t = 2, s = 8 - 32 + 40 = 16$	A1	1.1b
		(3)	
(c)	$s = 0 \Rightarrow t^3 - 8t^2 + 20t = 0$ and $t \neq 0 \Rightarrow t^2 - 8t + 20 = 0$	M1	2.1
	Explanation to show that $t^2 - 8t + 20 > 0$ for all t .	M1	2.4
	So $s = 0$ has no non-zero solutions, so s is never zero again, so never returns to O^*	A1*	3.2a
		(3)	
(8 marks)			
Notes:			
(a)			
M1: For multiplying out and differentiating (powers decreasing by 1)			
A1: For a correct expression for a			
(b)			
M1: For multiplying out and integrating (powers increasing by 1)			
A1: For a correct expression for s with or without C			
A1: For $C = 0$ and correct final answer			
(c)			
M1: For equating their s to 0 and producing a quadratic			
M1: For clear explanation that $t^2 - 8t + 20 > 0$ for all t (e.g. completing the square or another complete method)			
A1*: For a correct conclusion in context			

Question	Scheme	Marks	AOs
6(a)	$\cos \alpha = \frac{4}{5}$ or $\sin \alpha = \frac{3}{5}$	B1	1.1b
	$r = 4a \sin \alpha$	B1	1.1b
	Resolving vertically	M1	3.1b
	$T_1 \cos \alpha - T_2 \sin \alpha = mg$	A1	1.1b
	Resolving horizontally	M1	3.1b
	$T_1 \sin \alpha + T_2 \cos \alpha = m\omega^2$	A1	1.1b
	$T_1 \sin \alpha + T_2 \cos \alpha = m\omega^2$	A1	1.1b
	Solving for either tension	M1	2.1
	$T_1 = \frac{4m}{25}(9a\omega^2 + 5g)$ *	A1*	1.1b
	$T_2 = \frac{3m}{25}(16a\omega^2 - 5g)$ *	A1*	1.1b
		(10)	
(b)	$\frac{4m}{25}(9a\omega^2 + 5g) < 4mg$	M1	2.1
	$\frac{3m}{25}(16a\omega^2 - 5g) > 0$	M1	2.1
	$\omega > \sqrt{\frac{5g}{16a}}$ or $\omega < \sqrt{\frac{20g}{9a}}$	A1	2.2a
	$S = \frac{2\pi}{\omega}$	M1	1.1b
	$3\pi\sqrt{\frac{a}{5g}} < S < 8\pi\sqrt{\frac{a}{5g}}$ *	A1*	1.1b
		(5)	
(c)	String being light implies that the tension is constant in both portions of the string	B1	3.5b
		(1)	
(16 marks)			
Notes:			
<p>(a)</p> <p>B1: For correct trig. ratio seen</p> <p>B1: For a correct radius expression seen</p> <p>M1: For resolving vertically with correct no. of terms and tensions resolved</p> <p>A1: For a correct equation</p> <p>M1: For resolving horizontally with correct no. of terms and tensions resolved</p> <p>A1A1: For a correct equation</p> <p>M1: For solving their two equations to find either tension</p> <p>A1*: For the given answer</p> <p>A1*: For the given answer</p>			

Question 6 notes continued:

(b)

M1: For use of $T_1 < 4mg$

M1: For using $T_2 > 0$

A1: For a correct inequality (either) for ω

M1: For use of $S = \frac{2\pi}{\omega}$ with either critical value

A1*: For given answer

(c)

B1: For a clear explanation

Question	Scheme	Marks	AOs
7(a)	Rel. Mass: 2 5 1 8	B1	1.2
	$y:$ 2 0.5 1.5 \bar{y}	B1	1.2
	$x:$ 0.5 2.5 4.5 \bar{x}	B1	1.2
	$(2 \times 2) + (5 \times 0.5) + (1 \times 1.5) = 8\bar{y}$	M1	2.1
	$\bar{y} = 1 *$	A1*	1.1b
	$(2 \times 0.5) + (5 \times 2.5) + (1 \times 4.5) = 8\bar{x}$	M1	2.1
	$\bar{x} = 2.25$	A1	1.1b
	(7)		
(b)	Use of correct strategy to solve the problem by use of 'moments equation'	M1	3.1b
	$(8 \times 2.25) - (2\pi r^2 \times 0.5) = (8 - 2\pi r^2)2.5$	A1ft	1.1b
	Solving for r	M1	1.1b
	$r = \frac{1}{\sqrt{2\pi}} = 0.399$	A1	1.1b
	(4)		
(c)	Since \bar{y} for original plate is 1, holes must be symmetrically placed about the line $y = 1$	B1	2.4
	$a = 1.5$	B1	2.2a
	(2)		
(d)	Use of tan from an appropriate triangle	M1	1.1a
	$\tan \alpha = \frac{2}{1.5} = \frac{4}{3}$	A1ft	1.1b
	$\alpha = 53.1^\circ$	A1	1.1b
	(3)		
(16 marks)			
Notes:			
(a)			
B1: For correct relative masses			
B1: For correct y values			
B1: For correct x values			
M1: For a moments equation, correct no. of terms, condone sign errors			
A1*: For a correct given answer (1)			
M1: For a moments equation, correct no. of terms			
A1: For 2.25			
(b)			
M1: For a moments equation, correct no. of terms, condone sign errors			
A1ft: For a correct equation, follow through on their \bar{x}			
M1: For solving for r			
A1: For 0.399 or 0.40			

Question 7 notes continued:

(c)

B1: For consideration of symmetry about $y = 1$

B1: For $a = 1.5$

(d)

M1: For use of tan from an appropriate triangle

A1ft: For a correct equation, follow through on their a

A1: For a correct angle